Programming as Successive Refinement

Not all issues dealt with up front

Partitioning often independent of architecture, and done first

- View machine as a collection of communicating processors
  - balancing the workload
  - reducing the amount of inherent communication
  - reducing extra work
- Tug-o-war even among these three issues

Then interactions with architecture

- View machine as extended memory hierarchy
  - extra communication due to architectural interactions
  - cost of communication depends on how it is structured
- May inspire changes in partitioning

Discussion of issues is one at a time, but identifies tradeoffs

- Use examples, and measurements on SGI Origin2000

Partitioning for Performance

Balancing the workload and reducing wait time at synch points

Reducing inherent communication

Reducing extra work

Even these algorithmic issues trade off:

- Minimize comm. => run on 1 processor => extreme load imbalance
- Maximize load balance => random assignment of tiny tasks => no control over communication
- Good partition may imply extra work to compute or manage it

Goal is to compromise

- Fortunately, often not difficult in practice
Load Balance and Synch Wait Time

Limit on speedup: \[ Speedup_{\text{problem}}(p) \leq \frac{\text{Sequential Work}}{\text{Max Work on any Processor}} \]

- Work includes data access and other costs
- Not just equal work, but must be busy at same time

Four parts to load balance and reducing synch wait time:
1. Identify enough concurrency
2. Decide how to manage it
3. Determine the granularity at which to exploit it
4. Reduce serialization and cost of synchronization

Identifying Concurrency

Techniques seen for equation solver:
- Loop structure, fundamental dependences, new algorithms

Data Parallelism versus Function Parallelism

Often see orthogonal levels of parallelism; e.g. VLSI routing

(a) Wire \( W_2 \) expands to segments
(b) Segment \( S_3 \) expands to routes
(c)
Identifying Concurrency (contd.)

Function parallelism:
• entire large tasks (procedures) that can be done in parallel
• on same or different data
• e.g. different independent grid computations in Ocean
• pipelining, as in video encoding/decoding, or polygon rendering
• degree usually modest and does not grow with input size
• difficult to load balance
• often used to reduce synch between data parallel phases

Most scalable programs data parallel (per this loose definition)
• function parallelism reduces synch between data parallel phases

Deciding How to Manage Concurrency

Static versus Dynamic techniques

Static:
• Algorithmic assignment based on input; won’t change
• Low runtime overhead
• Computation must be predictable
• Preferable when applicable (except in multiprogrammed/heterogeneous environment)

Dynamic:
• Adapt at runtime to balance load
• Can increase communication and reduce locality
• Can increase task management overheads
Dynamic Assignment

Profile-based (semi-static):
- Profile work distribution at runtime, and repartition dynamically
- Applicable in many computations, e.g. Barnes-Hut, some graphics

Dynamic Tasking:
- Deal with unpredictability in program or environment (e.g. Raytrace)
  - computation, communication, and memory system interactions
  - multiprogramming and heterogeneity
  - used by runtime systems and OS too
- Pool of tasks; take and add tasks until done
- E.g. “self-scheduling” of loop iterations (shared loop counter)

Dynamic Tasking with Task Queues

Centralized versus distributed queues

Task stealing with distributed queues
- Can compromise comm and locality, and increase synchronization
- Whom to steal from, how many tasks to steal, ...
- Termination detection
- Maximum imbalance related to size of task

![Diagram of task queues](image)
Impact of Dynamic Assignment

On SGI Origin 2000 (cache-coherent shared memory):

Determining Task Granularity

Task granularity: amount of work associated with a task

General rule:
- Coarse-grained => often less load balance
- Fine-grained => more overhead; often more comm., contention

Comm., contenton actually affected by assignment, not size
- Overhead by size itself too, particularly with task queues
Reducing Serialization

Careful about assignment and orchestration (including scheduling)

Event synchronization
- Reduce use of conservative synchronization
  - e.g. point-to-point instead of barriers, or granularity of pt-to-pt
- But fine-grained synch more difficult to program, more synch ops.

Mutual exclusion
- Separate locks for separate data
  - e.g. locking records in a database: lock per process, record, or field
  - lock per task in task queue, not per queue
  - finer grain => less contention/serialization, more space, less reuse
- Smaller, less frequent critical sections
  - don’t do reading/testing in critical section, only modification
  - e.g. searching for task to dequeue in task queue, building tree
- Stagger critical sections in time

Implications of Load Balance

Extends speedup limit expression to: \[ \frac{\text{Sequential Work}}{\max(\text{Work} + \text{Synch Wait Time})} \leq 1 \]

Generally, responsibility of software

Architecture can support task stealing and synch efficiently
- Fine-grained communication, low-overhead access to queues
  - efficient support allows smaller tasks, better load balance
- Naming logically shared data in the presence of task stealing
  - need to access data of stolen tasks, esp. multiply-stolen tasks
- => Hardware shared address space advantageous
- Efficient support for point-to-point communication
Reducing Inherent Communication

Communication is expensive!

Measure: *communication to computation ratio*

Focus here on inherent communication
- Determined by assignment of tasks to processes
- Later see that actual communication can be greater

Assign tasks that access same data to same process

Solving communication and load balance NP-hard in general case
But simple heuristic solutions work well in practice
- Applications have structure!

Domain Decomposition

Works well for scientific, engineering, graphics, ... applications

Exploits local-biased nature of physical problems
- Information requirements often short-range
- Or long-range but fall off with distance

Simple example: nearest-neighbor grid computation

Perimeter to Area comm-to-comp ratio (area to volume in 3-d)
- Depends on \( n, p \): decreases with \( n \), increases with \( p \)
Domain Decomposition (contd)

Best domain decomposition depends on information requirements

Nearest neighbor example: block versus strip decomposition:

Comm to comp: \( \frac{d \times P}{n} \) for block, \( \frac{2 \times P}{n} \) for strip

- Retain block from here on

Application dependent: strip may be better in other cases

  - E.g. particle flow in tunnel

Finding a Domain Decomposition

Static, by inspection
  - Must be predictable: grid example above, and Ocean

Static, but not by inspection
  - Input-dependent, require analyzing input structure
  - E.g sparse matrix computations, data mining (assigning itemsets)

Semi-static (periodic repartitioning)
  - Characteristics change but slowly; e.g. Barnes-Hut

Static or semi-static, with dynamic task stealing
  - Initial decomposition, but highly unpredictable; e.g ray tracing
Implications of Comm-to-Comp Ratio

Architects examine application needs to see where to spend money
If denominator is execution time, ratio gives average BW needs
If operation count, gives extremes in impact of latency and bandwidth
  • Latency: assume no latency hiding
  • Bandwidth: assume all latency hidden
  • Reality is somewhere in between
Actual impact of comm. depends on structure and cost as well
  \[
  \text{Speedup} \leq \frac{\text{Sequential Work}}{\max(\text{Work} + \text{Synch Wait Time} + \text{Comm Cost})}
  \]
  • Need to keep communication balanced across processors as well

Reducing Extra Work

Common sources of extra work:
  • Computing a good partition
    – e.g. partitioning in Barnes-Hut or sparse matrix
  • Using redundant computation to avoid communication
  • Task, data and process management overhead
    – applications, languages, runtime systems, OS
  • Imposing structure on communication
    – coalescing messages, allowing effective naming
Architectural Implications:
  • Reduce need by making communication and orchestration efficient
  \[
  \text{Speedup} \leq \frac{\text{Sequential Work}}{\max(\text{Work} + \text{Synch Wait Time} + \text{Comm Cost} + \text{Extra Work})}
  \]
**What is a Multiprocessor?**

A collection of communicating processors
- View taken so far
- Goals: balance load, reduce inherent communication and extra work

A multi-cache, multi-memory system
- Role of these components essential regardless of programming model
- Prog. model and comm. abstr. affect specific performance tradeoffs

Most of remaining perf. issues focus on second aspect

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**Memory-oriented View**

Multiprocessor as Extended Memory Hierarchy
- as seen by a given processor

Levels in extended hierarchy:
- Registers, caches, local memory, remote memory (topology)
- Glued together by communication architecture
- Levels communicate at a certain granularity of data transfer

Need to exploit spatial and temporal locality in hierarchy
- Otherwise extra communication may also be caused
- Especially important since communication is expensive
Uniprocessor

Performance depends heavily on memory hierarchy

Time spent by a program

\[ Time_{prog}(1) = Busy(1) + Data \text{ Access}(1) \]

• Divide by cycles to get CPI equation

Data access time can be reduced by:

• Optimizing machine: bigger caches, lower latency...
• Optimizing program: temporal and spatial locality

Extended Hierarchy

Idealized view: local cache hierarchy + single main memory

But reality is more complex

• Centralized Memory: caches of other processors
• Distributed Memory: some local, some remote; + network topology
• Management of levels
  – caches managed by hardware
  – main memory depends on programming model
    • SAS: data movement between local and remote transparent
    • message passing: explicit
• Levels closer to processor are lower latency and higher bandwidth
• Improve performance through architecture or program locality
• Tradeoff with parallelism; need good node performance and parallelism
Artifactual Comm. in Extended Hierarchy

Accesses not satisfied in local portion cause communication
• Inherent communication, implicit or explicit, causes transfers
  – determined by program
• Artifactual communication
  – determined by program implementation and arch. interactions
  – poor allocation of data across distributed memories
  – unnecessary data in a transfer
  – unnecessary transfers due to system granularities
  – redundant communication of data
  – finite replication capacity (in cache or main memory)
• Inherent communication assumes unlimited capacity, small transfers, perfect knowledge of what is needed.
• More on artifactual later; first consider replication-induced further

Communication and Replication

Comm induced by finite capacity is most fundamental artifact
• Like cache size and miss rate or memory traffic in uniprocessors
• Extended memory hierarchy view useful for this relationship

View as three level hierarchy for simplicity
• Local cache, local memory, remote memory (ignore network topology)

Classify “misses” in “cache” at any level as for uniprocessors
  – compulsory or cold misses (no size effect)
  – capacity misses (yes)
  – conflict or collision misses (yes)
  – communication or coherence misses (no)
• Each may be helped/hurt by large transfer granularity (spatial locality)
Orchestration for Performance

Reducing amount of communication:
  • Inherent: change logical data sharing patterns in algorithm
  • Artifactual: exploit spatial, temporal locality in extended hierarchy
    – Techniques often similar to those on uniprocessors

Structuring communication to reduce cost

Let’s examine techniques for both...

Reducing Artifactual Communication

Message passing model
  • Communication and replication are both explicit
  • Even artifactual communication is in explicit messages

Shared address space model
  • More interesting from an architectural perspective
  • Occurs transparently due to interactions of program and system
    – sizes and granularities in extended memory hierarchy

Use shared address space to illustrate issues
Exploiting Temporal Locality

- Structure algorithm so working sets map well to hierarchy
  - often techniques to reduce inherent communication do well here
  - schedule tasks for data reuse once assigned
- Multiple data structures in same phase
  - e.g. database records: local versus remote
- Solver example: blocking

- More useful when $O(n^{k+1})$ computation on $O(n^k)$ data
  - many linear algebra computations (factorization, matrix multiply)

Exploiting Spatial Locality

Besides capacity, granularities are important:
- Granularity of allocation
- Granularity of communication or data transfer
- Granularity of coherence

Major spatial-related causes of artifactual communication:
- Conflict misses
- Data distribution/layout (allocation granularity)
- Fragmentation (communication granularity)
- False sharing of data (coherence granularity)

All depend on how spatial access patterns interact with data structures
- Fix problems by modifying data structures, or layout/alignment

Examine later in context of architectures
- one simple example here: data distribution in SAS solver
**Spatial Locality Example**

- Repeated sweeps over 2-d grid, each time adding 1 to elements
- Natural 2-d versus higher-dimensional array representation

![Contiguity in memory layout](image)

- Page straddles partition boundaries: difficult to distribute memory well
- Cache block straddles partition boundary
- Page does not straddle partition boundary
- Cache block is within a partition

(a) Two-dimensional array

(b) Four-dimensional array

**Tradeoffs with Inherent Communication**

Partitioning grid solver: blocks versus rows

- Blocks still have a spatial locality problem on remote data
- Rowwise can perform better despite worse inherent c-to-c ratio

![Contiguity in memory layout](image)

- Good spatial locality on nonlocal accesses at row-oriented boundary
- Poor spatial locality on nonlocal accesses at column-oriented boundary

- Result depends on $n$ and $p$
Example Performance Impact

Equation solver on SGI Origin2000

Architectural Implications of Locality

Communication abstraction that makes exploiting it easy

For cache-coherent SAS, e.g.:
- Size and organization of levels of memory hierarchy
  - cost-effectiveness: caches are expensive
  - caveats: flexibility for different and time-shared workloads
- Replication in main memory useful? If so, how to manage?
  - hardware, OS/runtime, program?
- Granularities of allocation, communication, coherence (?)
  - small granularities => high overheads, but easier to program

Machine granularity (resource division among processors, memory...
**Structuring Communication**

Given amount of comm (inherent or artifactual), goal is to reduce cost

Cost of communication as seen by process:

\[
C = f \times (o + l + \frac{n_c}{m} + t_c - \text{overlap})
\]

- \(f\) = frequency of messages
- \(o\) = overhead per message (at both ends)
- \(l\) = network delay per message
- \(n_c\) = total data sent
- \(m\) = number of messages
- \(B\) = bandwidth along path (determined by network, NI, assist)
- \(t_c\) = cost induced by contention per message
- \(\text{overlap}\) = amount of latency hidden by overlap with comp. or comm.

- Portion in parentheses is cost of a message (as seen by processor)
- That portion, ignoring overlap, is latency of a message
- Goal: reduce terms in latency and increase overlap

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**Reducing Overhead**

Can reduce no. of messages \(m\) or overhead per message \(o\)

\(o\) is usually determined by hardware or system software

- Program should try to reduce \(m\) by coalescing messages
- More control when communication is explicit

Coalescing data into larger messages:

- Easy for regular, coarse-grained communication
- Can be difficult for irregular, naturally fine-grained communication
  - may require changes to algorithm and extra work
    - coalescing data and determining what and to whom to send
  - will discuss more in implications for programming models later
Reducing Network Delay

Network delay component = \( f h t_h \)
- \( h \) = number of hops traversed in network
- \( t_h \) = link+switch latency per hop

Reducing \( f \): communicate less, or make messages larger

Reducing \( h \):
- Map communication patterns to network topology
  - e.g. nearest-neighbor on mesh and ring; all-to-all
- How important is this?
  - used to be major focus of parallel algorithms
  - depends on no. of processors, how \( t_h \) compares with other components
  - less important on modern machines
    - overheads, processor count, multiprogramming

Reducing Contention

All resources have nonzero occupancy
- Memory, communication controller, network link, etc.
- Can only handle so many transactions per unit time

Effects of contention:
- Increased end-to-end cost for messages
- Reduced available bandwidth for individual messages
- Causes imbalances across processors

Particularly insidious performance problem
- Easy to ignore when programming
- Slow down messages that don’t even need that resource
  - by causing other dependent resources to also congest
- Effect can be devastating: *Don’t flood a resource!*
**Types of Contention**

Network contention and end-point contention (*hot-spots*)

*Location and Module Hot-spots*
- Location: e.g. accumulating into global variable, barrier
  - solution: tree-structured communication
- Module: all-to-all personalized comm. in matrix transpose
  - solution: stagger access by different processors to same node temporally
- In general, reduce burstiness; may conflict with making messages larger

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**Overlapping Communication**

Cannot afford to stall for high latencies
- even on uniprocessors!

Overlap with computation or communication to hide latency

Requires extra concurrency (*slackness*), higher bandwidth

Techniques:
- Prefetching
- Block data transfer
- Proceeding past communication
- Multithreading
Summary of Tradeoffs

Different goals often have conflicting demands

• **Load Balance**
  – fine-grain tasks
  – random or dynamic assignment

• **Communication**
  – usually coarse grain tasks
  – decompose to obtain locality: not random/dynamic

• **Extra Work**
  – coarse grain tasks
  – simple assignment

• **Communication Cost:**
  – big transfers: amortize overhead and latency
  – small transfers: reduce contention